

# Analyzing the spectrum with functional data analysis

Rasmus Puggaard-Rode



**We have the tools to statistically model spectral shape directly, and doing so forgoes some of the problems with other methods of describing the spectrum**



# Roadmap

- The case: Danish /t/ releases
- Analyzing aperiodic spectra
  - FDA as an alternative
- Two corpus studies
  - Affrication in Modern Standard Danish
    - Function-on-scalar regression
  - Affrication in traditional Jutland Danish varieties
    - Functional principal component analysis
- General discussion

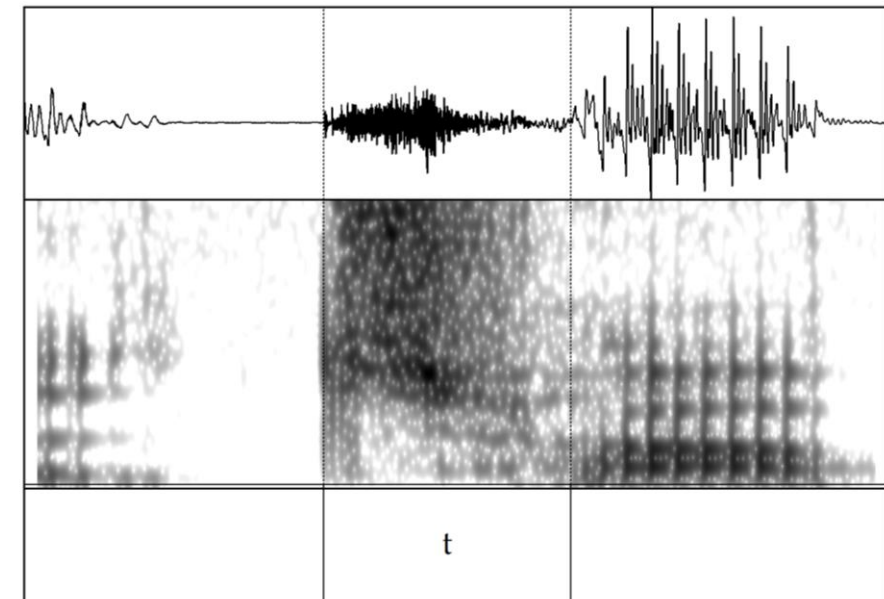
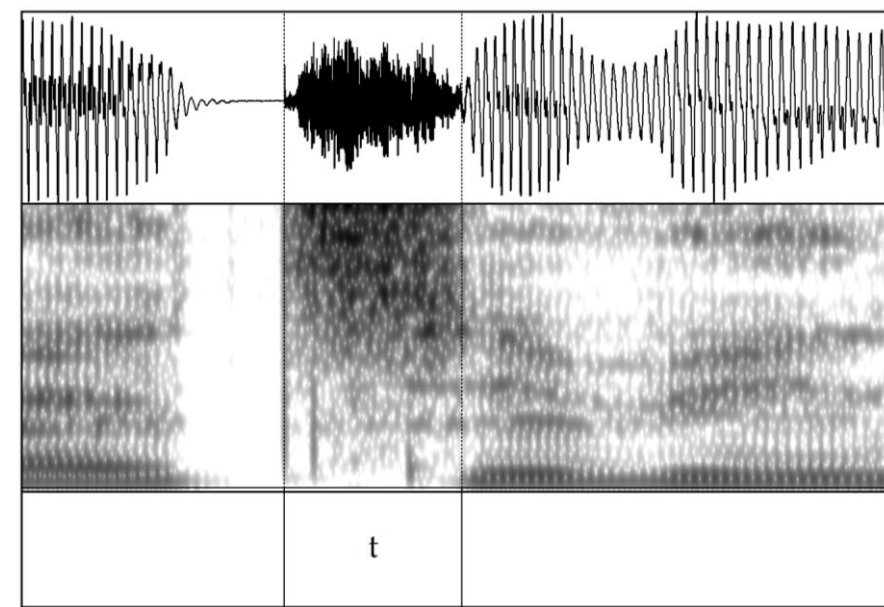


# Danish /t/ releases

- Modern Standard Danish has an aspiration-based laryngeal contrast in stops
  - Unaspirated /b d g/
  - Aspirated /p t k/
- /t/ is saliently affricated
  - Aspirated stop? Affricated stop? Affricate?
- Transcription strategies
  - [d̥<sup>s</sup>] (Basbøll 1969, 2005; Grønnum 1998)
  - [d̥<sup>sh</sup>] (Petersen 1983)
  - [d̥<sup>sh</sup>] (Brink & Lund 1975)
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  - [ts] (Schachtenhaufen 2022)

# Danish /t/ releases

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- /t/ is saliently affricated. What is it?
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# Danish /t/ releases

- Fischer-Jørgensen (1954, 1972)
  - /t/ releases contain both affrication and aspiration proper
  - The affrication spectrum is similar to the /s/ spectrum
  - Superimposing /t/ aspiration on /p k/ will lead listeners to perceive the sound as /t/
- Brink & Lund (1975)
  - /t/ affrication was widespread in mid-19C in Copenhagen
  - In mid-20C it was exceptionless in Copenhagen

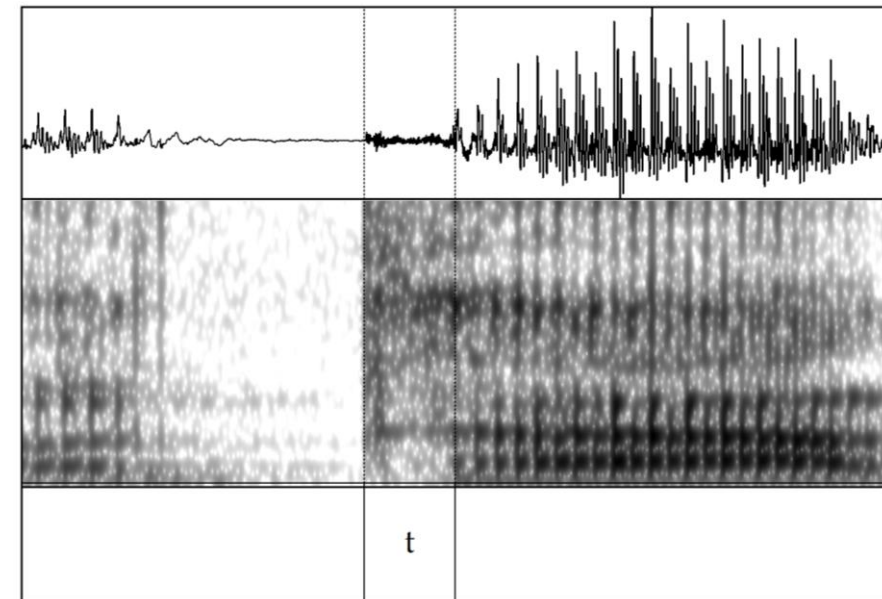
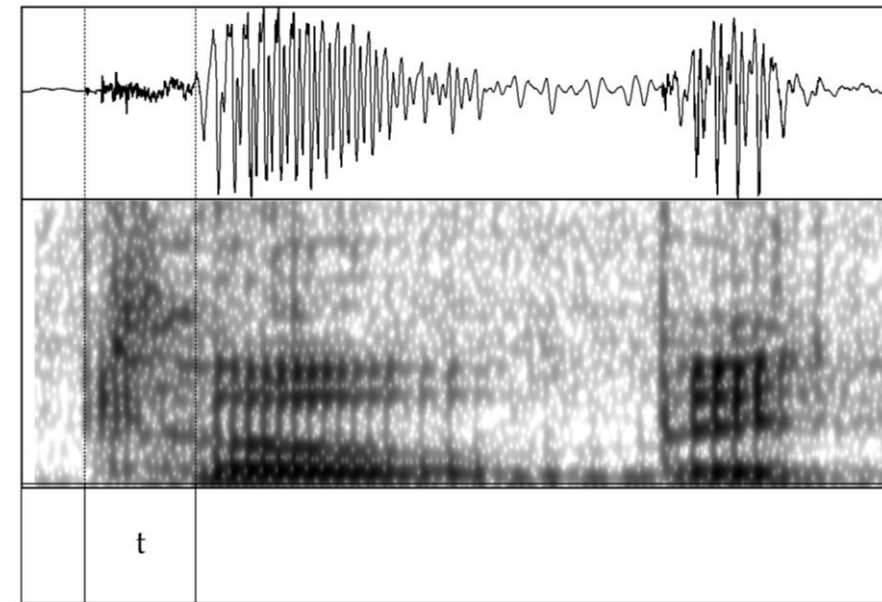
# Variation

- Not all varieties have saliently affricated /t/
- **But** it's a complete mystery which varieties lack it
  - Missing from
    - 'All dialects' (Brink & Lund 1975)
    - High and formal styles (Grønnum 2005)
    - Northern Jutlandic (Petersen 2009)
    - Western Jutlandic (Petersen et al. 2021)
    - All Jutland varieties except Eastern Jutlandic (Heger 1981)
- The sociolinguistic situation of Danish dialects is complex, but these traditional varieties are presumably (nearly) extinct (Pedersen 2003; but see also Maegaard & Monka 2019)



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# Who cares?

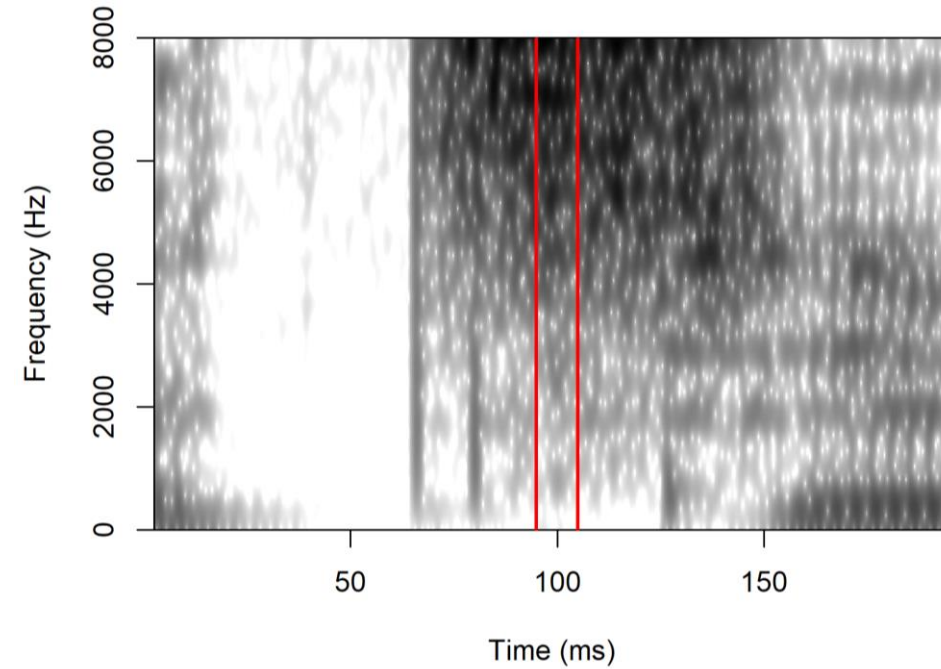
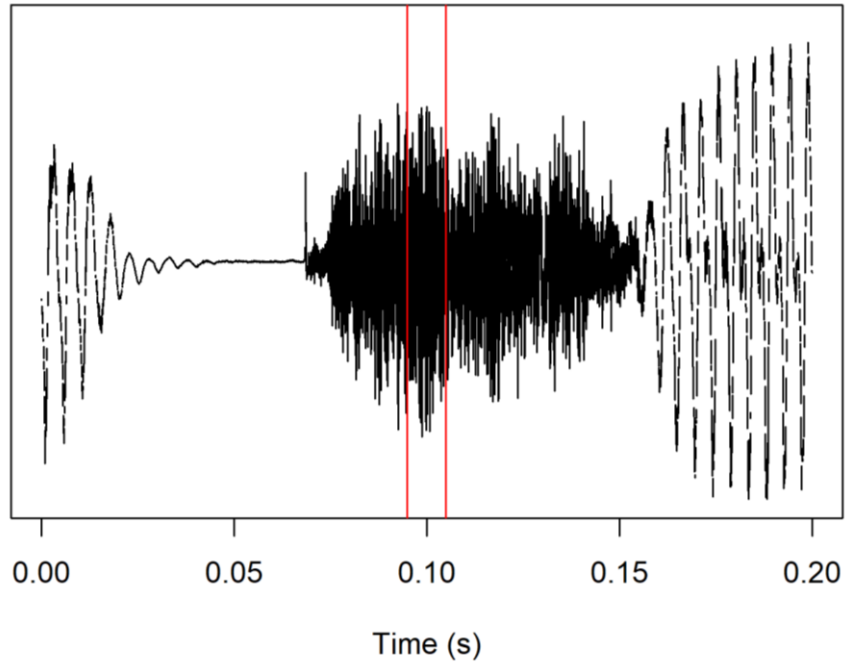
- These are unresolved issues in a very well-described language
  - But too often they're treated as solved
- How much does fine phonetic detail vary?
- What governs variation in fine phonetic detail?

**RQ1: How do spectral characteristics vary over time in Modern Standard Danish /t/ releases, and how are they affected by phonetic context?**

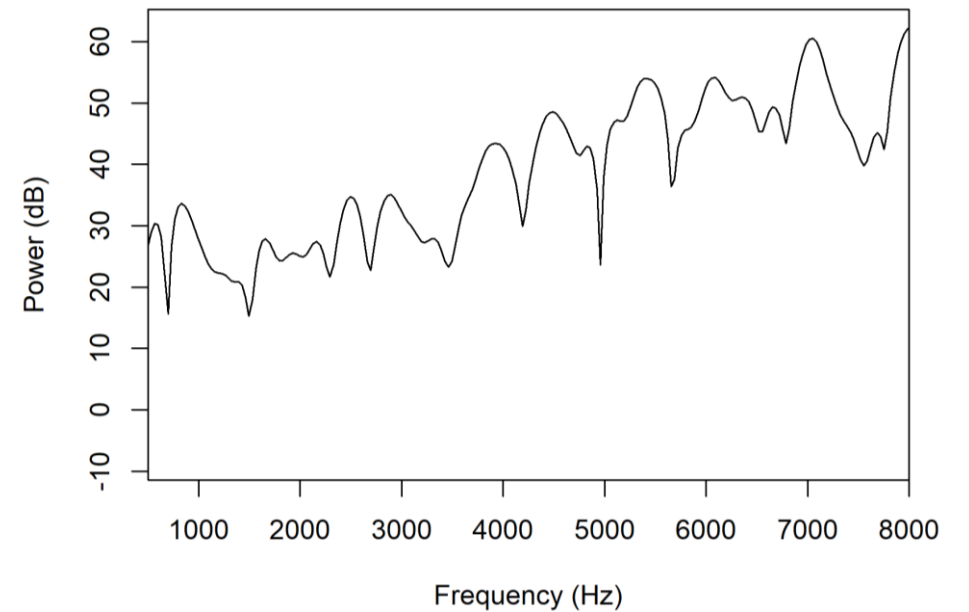
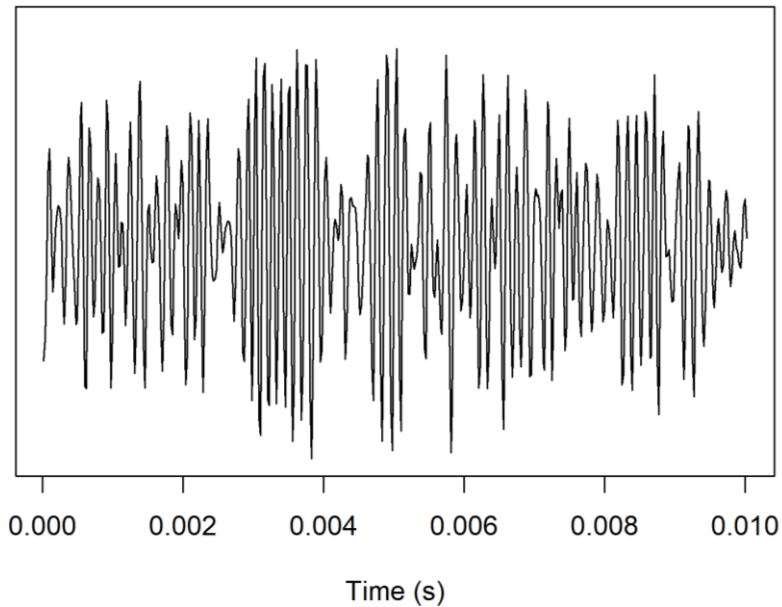
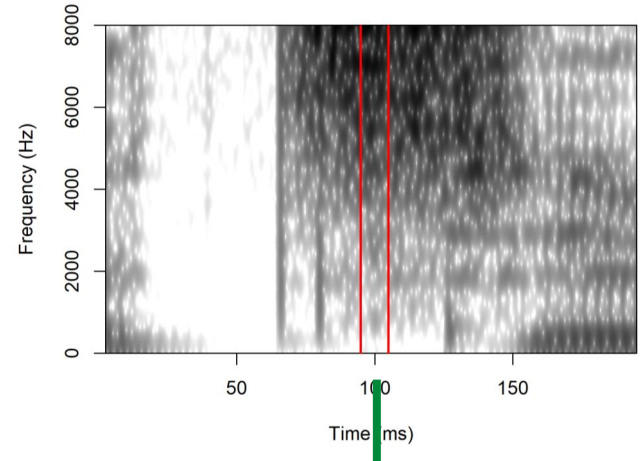
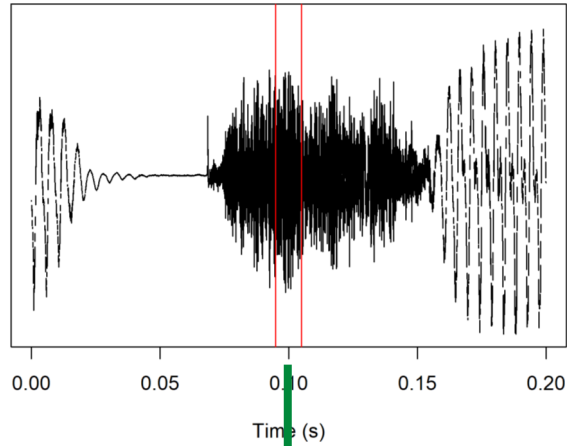
**RQ2: How do spectral characteristics of /t/ releases vary geographically in traditional dialects of Jutland?**



# Aperiodic spectra

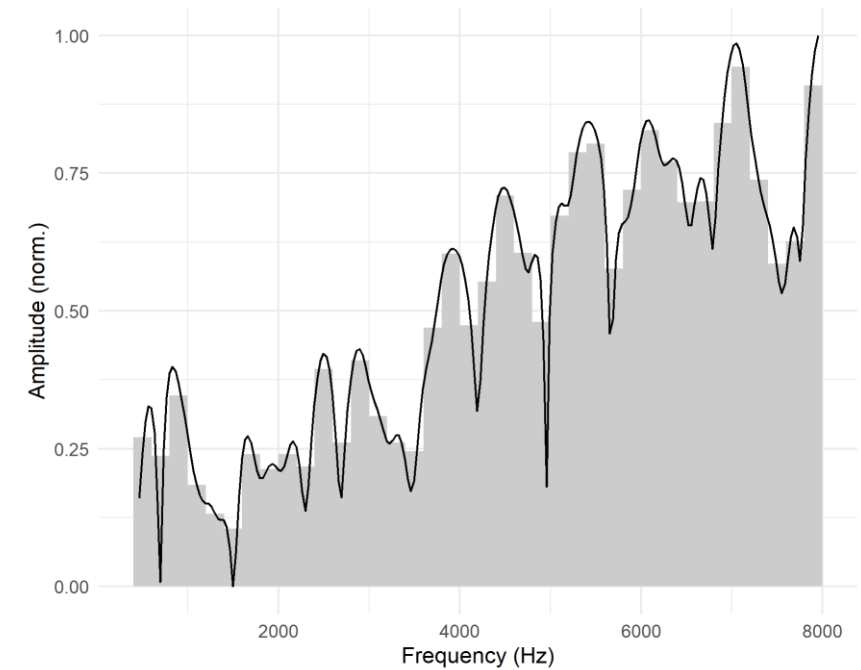


# Aperiodic spectra



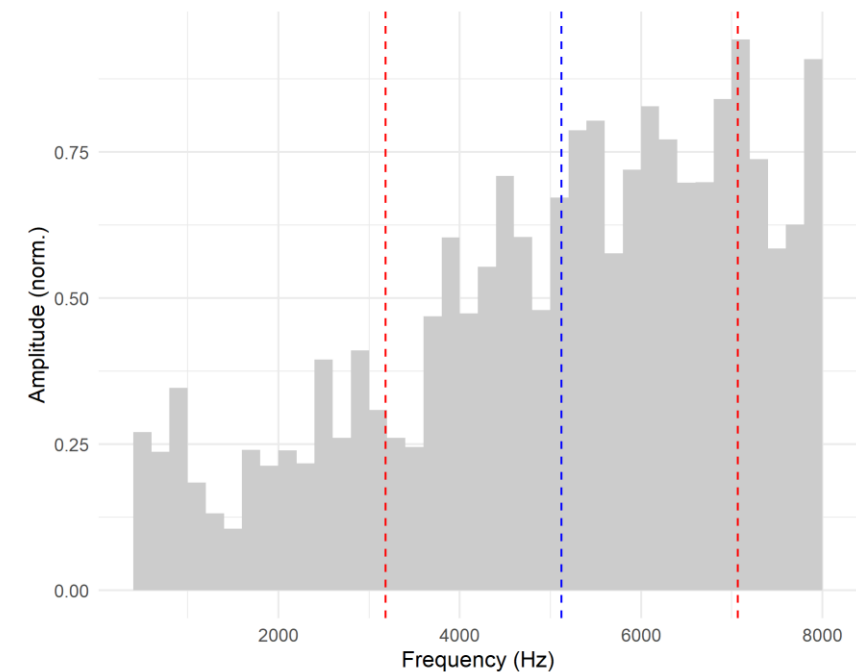
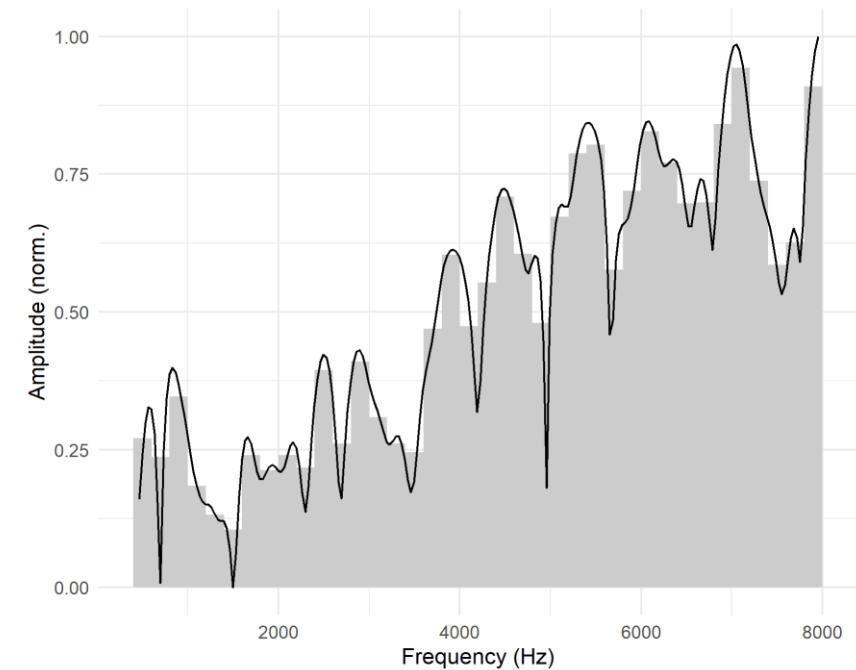
# Spectral moments

- Treating the spectrum as a probability distribution, and deriving moments from it (Forrest et al. 1988)



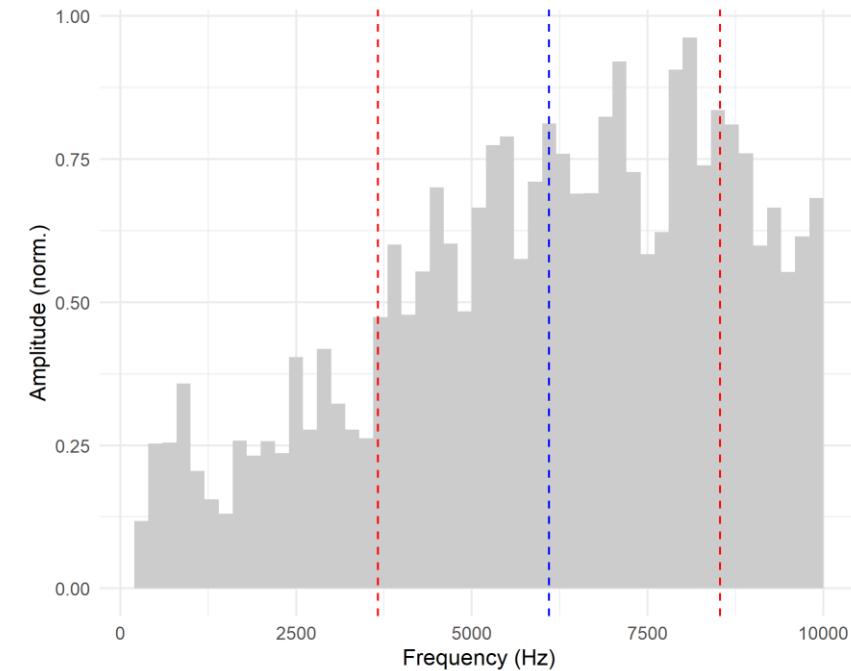
# Spectral moments

- Treating the spectrum as a probability distribution, and deriving moments from it (Forrest et al. 1988)
  - Centroid frequency, or **center of gravity**
    - 5,124 Hz
  - Standard deviation
    - 1,941 Hz
  - Skewness
    - -1.2
  - Kurtosis
    - 1.36



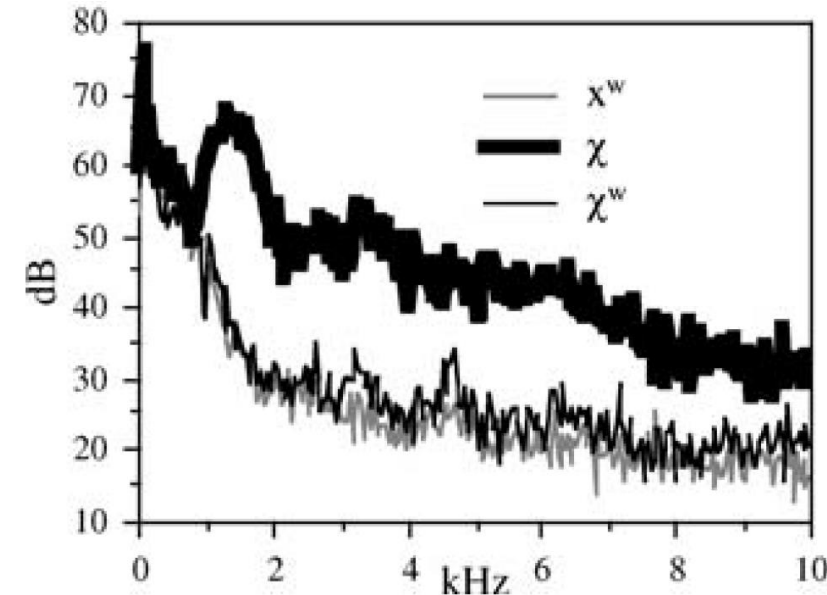
# Spectral moments

- Subsequent studies have not given consistent results about which moments are useful  
(Stoel-Gammon et al. 1994; Shadle & Mair 1996)
- Spectral moments are highly dependent on how the spectrum is filtered
  - Our spectrum was filtered at 500–8,000 Hz
  - If we'd chosen 300–10,000 Hz instead
    - COG would be ~1,000 Hz higher
    - SD would be ~500 Hz higher



# Spectral moments

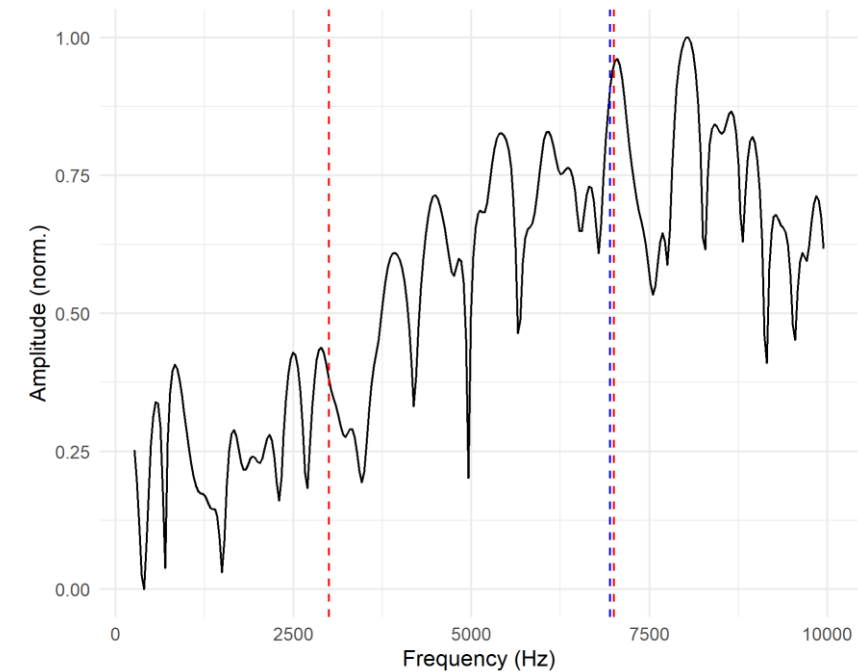
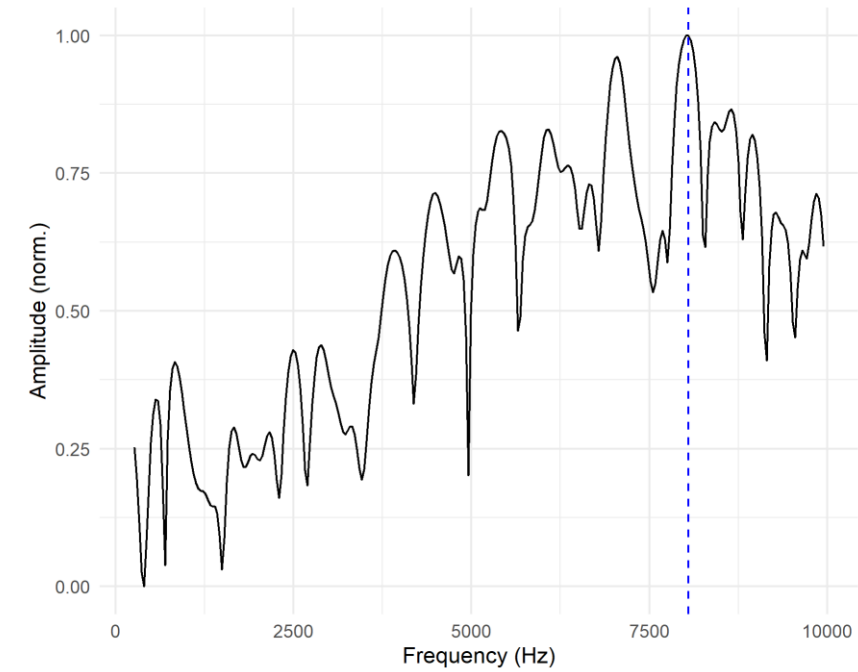
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  - If we'd chosen 300–10,000 Hz instead
    - COG would be ~1,000 Hz higher
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- Higher moments are often ignored, and **COG alone says little about spectral shape**
  - $[\chi \chi^w]$  have roughly identical COG in Montana Salish





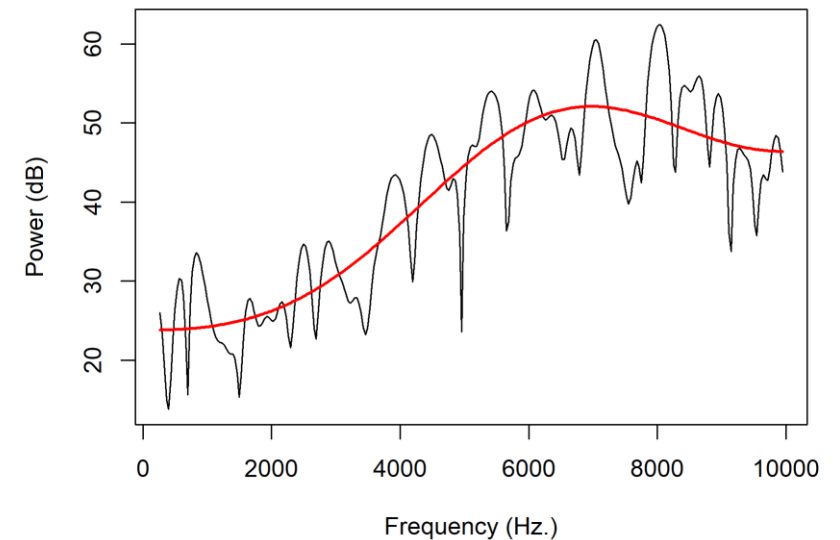
# Peak frequency

- Peak frequency (Jongman et al. 2000)
  - 8,050 Hz
  
- Mid-frequency spectral peak (Koenig et al. 2013; Chodroff & Wilson 2022)
  - 6,952 Hz



# DCT coefficients

- Smoothing aperiodic spectra with four DCTs usually **retains gross spectral shape** (Bunnell et al. 2004; Harrington 2010; Spinu & Lilley 2016; Jannedy and Weirich 2017; Kokkelmans 2021)
  - DCT coefficients then tell us something about
    - Mean ( $k_0$ )
    - Slope ( $k_1$ )
    - Curvature ( $k_2$ )
    - Amplitude at higher frequencies ( $k_3$ )



**LMU**

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MÜNCHEN

**We need to operationalize RQ1 and RQ2,  
but we are now lost in the  
garden of forking paths**

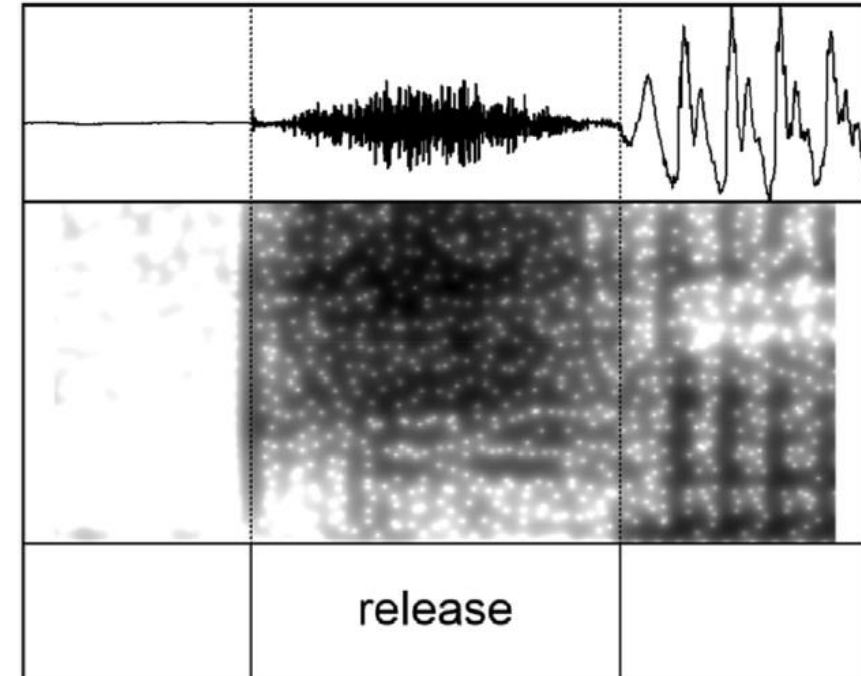


# Functional data analysis

- Extensions of statistical methods for functional data  
(Ramsay & Silverman 2005; Kokoszka & Reimherr 2017)
  - Functional PCA (Gubian et al. 2015)
  - Functional regression models (Greven & Scheipl 2017; Pouplier et al. 2017)
- Often applied to time series data  $Y(t)$ 
  - But should work just as well for spectral data  $A(f)$

# RQ1: Materials

- Monologs from DanPASS corpus (Grønnum 2009)
  - ~3 hours of speech, 18 speakers (5F/13M)
  - 850 /t/ tokens
    - Mean VOT: 79 ms (stressed), 68 ms (unstressed)
- Each stop split into 20 normalized time steps
  - Multitaper spectra generated in R for each of these
  - Frequency range 500–10,000 Hz



# Function-on-scalar regression

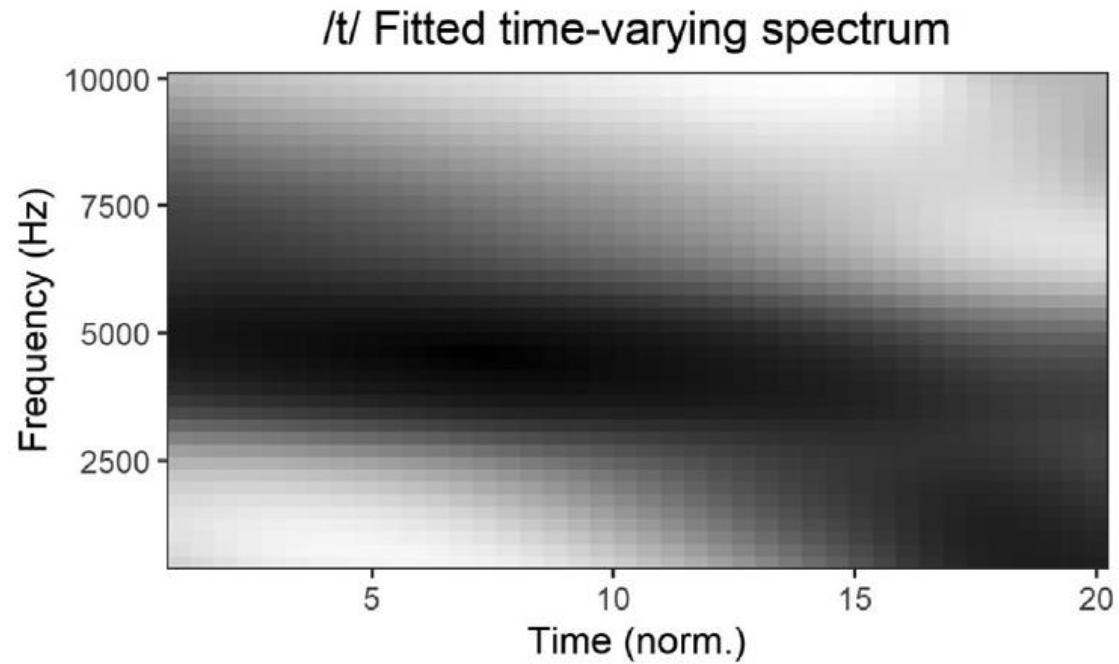
- Modeled with **function-on-scalar** models fitted with `refund::pfr` (Bauer et al. 2018; Goldsmith et al. 2021)
  - Wrapper for `mgcv` functions, so won't be totally unfamiliar for GAMM users (Wood 2017)
  - Allows problems to be formalized as functional regression
- GAMM: amplitude  $\sim$  frequency  $\times$  time ☹️
- FOSR: spectrum  $\sim$  time 😊

# Function-on-scalar regression

- Model structure
  - The spectrum has a smooth functional intercept
  - Spectral shape can vary smoothly over time
  - For each of the following fixed effects, spectra can vary smoothly over time
    - Speaker sex
    - Following vowel height, roundness, backness
    - Stress
  - By-speaker functional random slopes for each fixed effect
  - Corrected for autocorrelated errors

```
pffr(Y ~ s(timestep, k=16) +
      s(timestep, k=16, by=stressn) +
      s(timestep, k=16, by=sexn) +
      s(timestep, k=16, by=high_vn) +
      s(timestep, k=16, by=back_vn) +
      s(timestep, k=16, by=round_vn) +
      s(speaker, timestep, bs="re") +
      s(speaker, timestep, by=stressn, bs="re") +
      s(speaker, timestep, by=high_vn, bs="re") +
      s(speaker, timestep, by=back_vn, bs="re") +
      s(speaker, timestep, by=round_vn, bs="re"),
  data=t_df, ydata=t_y,
  bs.yindex = list(bs="ps", k=6, m=c(2,1)),
  bs.int = list(bs="ps", k=round(nrow(t_y) / nrow(t_df), 0), m=c(2,1)),
  rho = ar1+0.1,
```

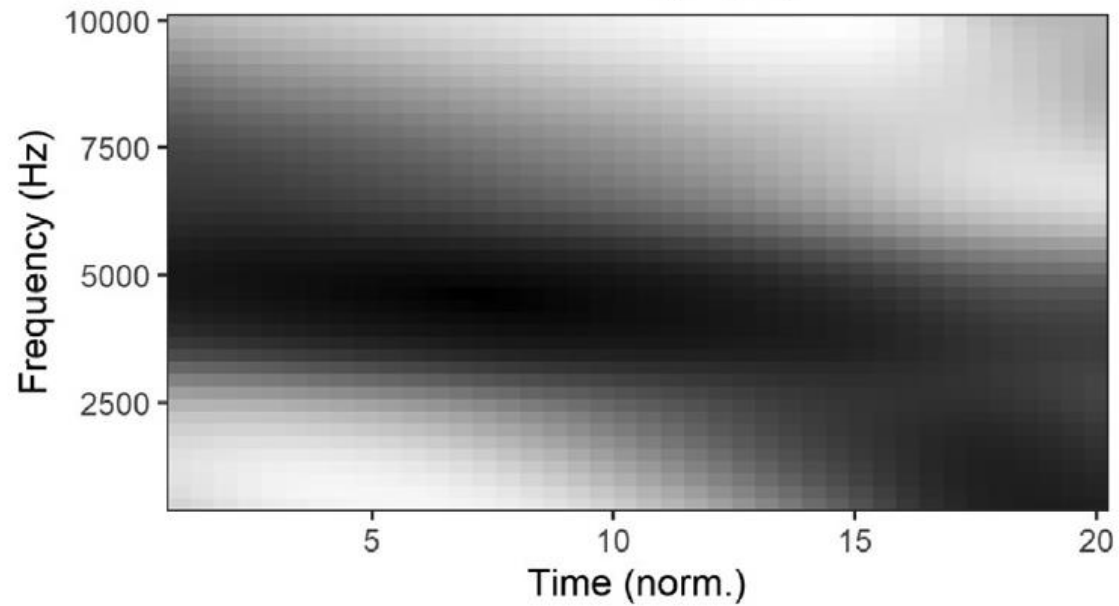
# Results



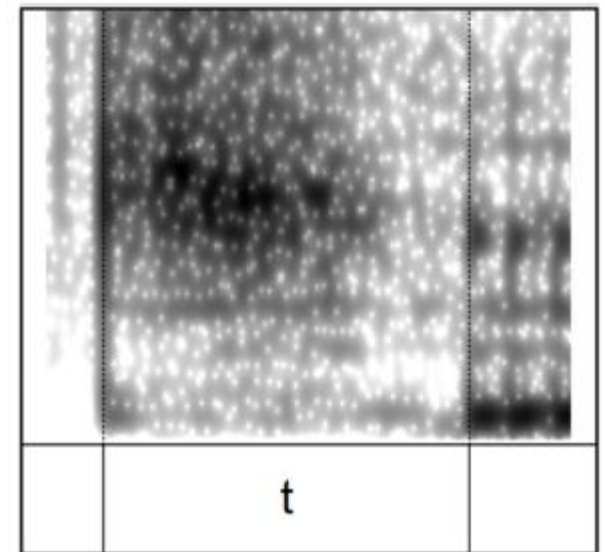


# Results

/t/ Fitted time-varying spectrum

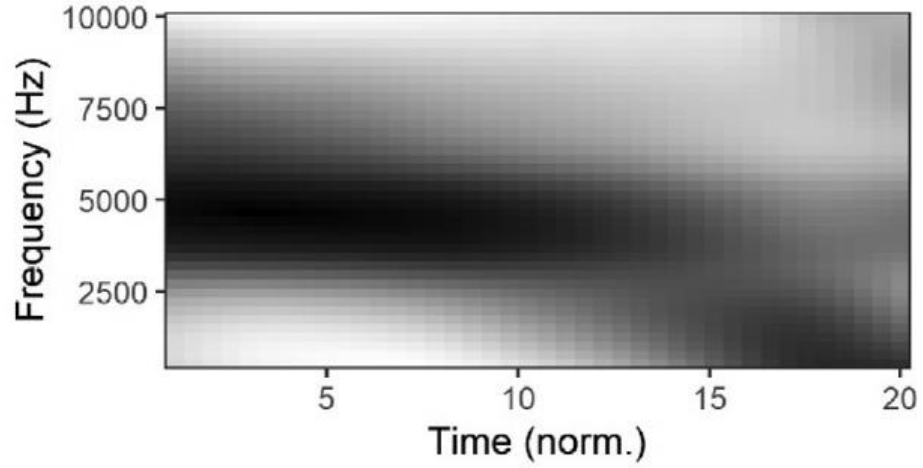


cp. a real spectrogram

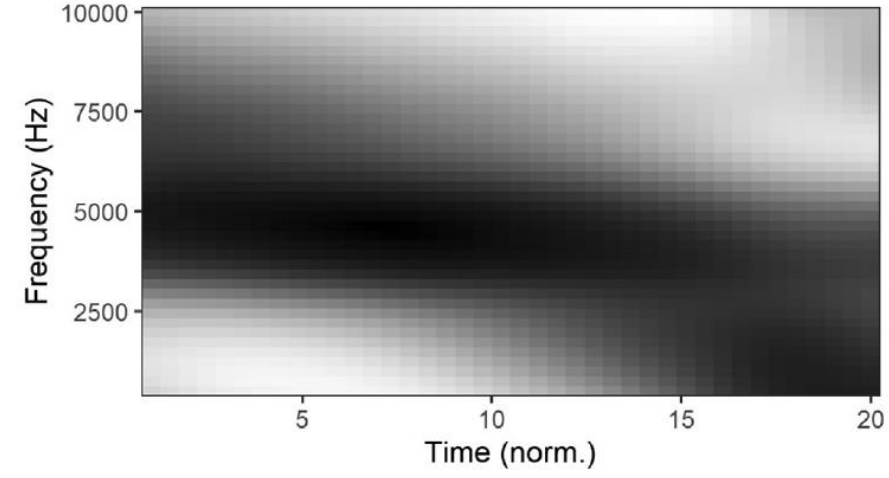


# Results

/t/ Men

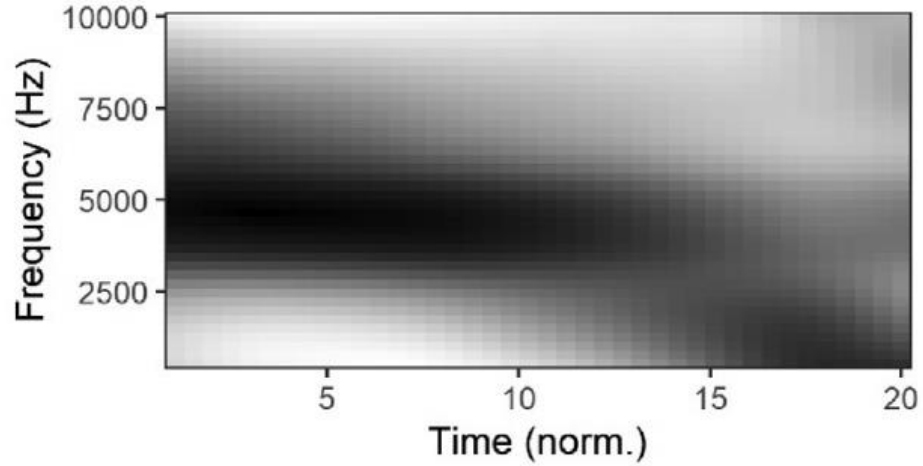


/t/ Fitted time-varying spectrum

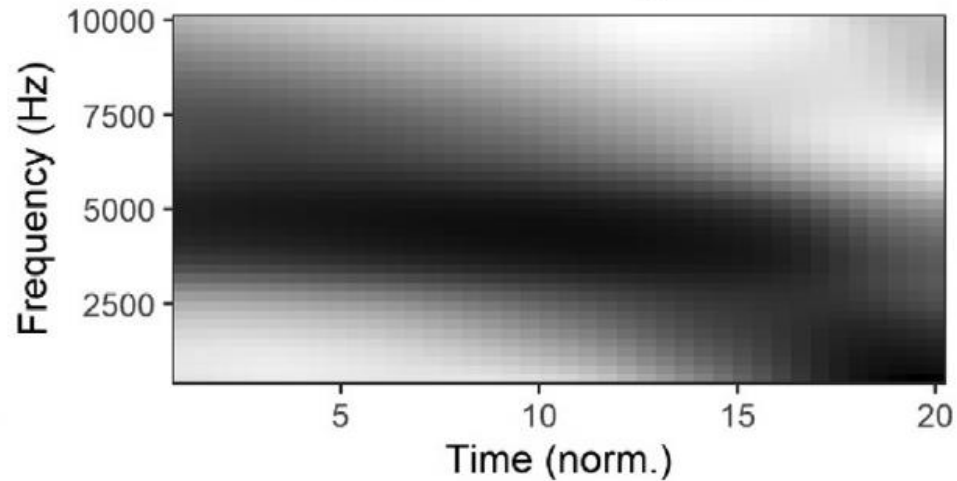


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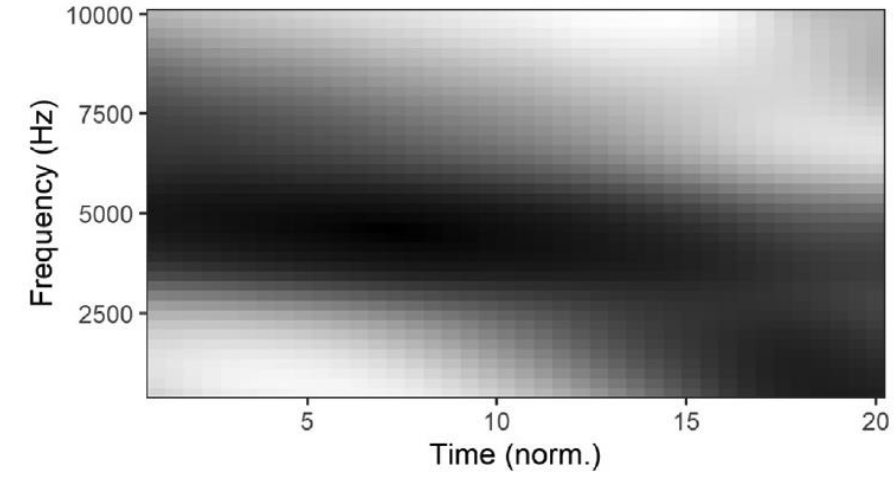
/t/ Men



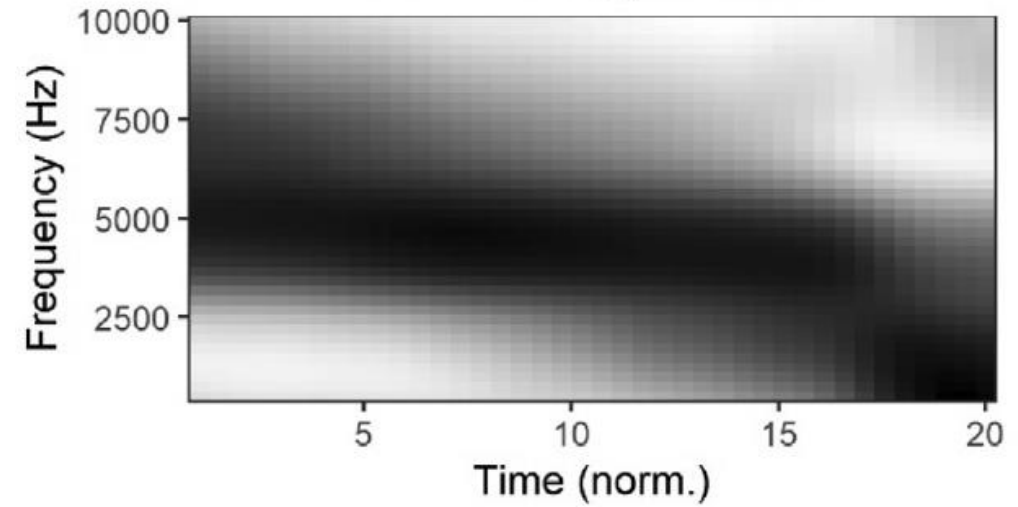
/t/ Unstressed syllables



/t/ Fitted time-varying spectrum

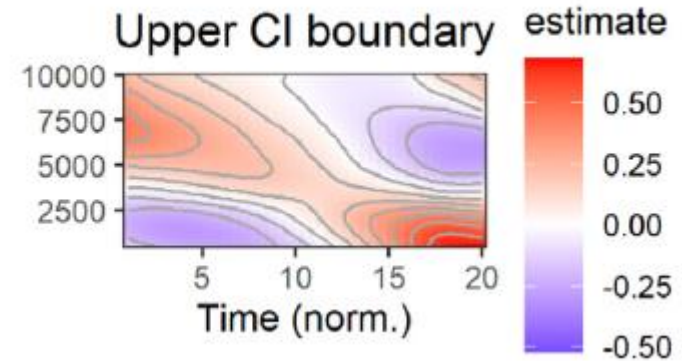
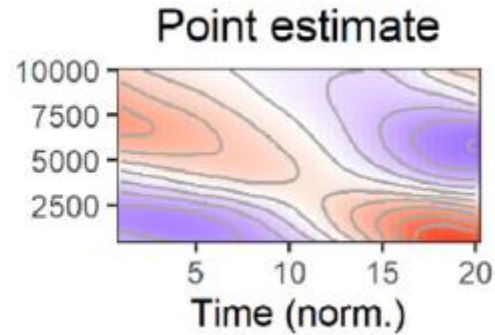
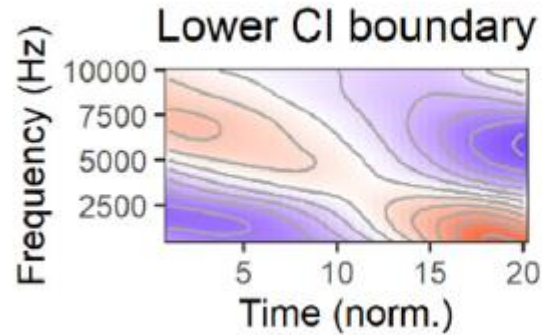


/t/ Before high vowels

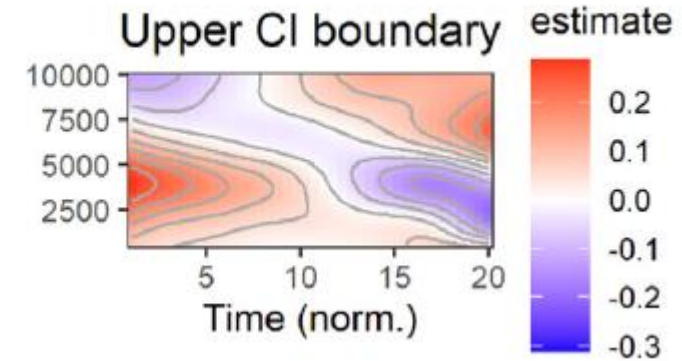
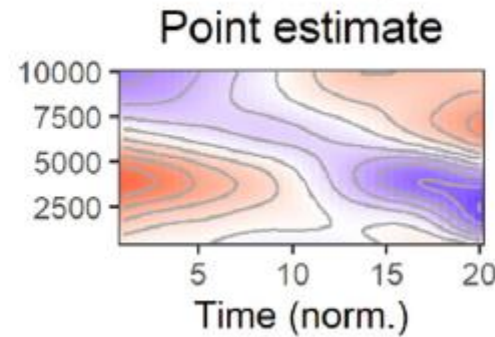
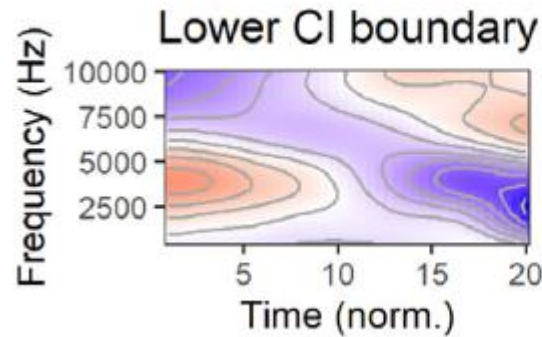


# Results

## /t/ Main effect of time



## /t/ Sex: -F, +M

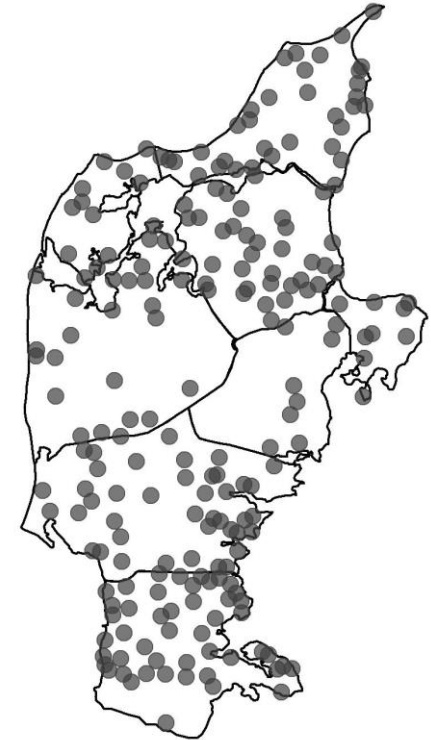


# Interim discussion

- MSD /t/ is invariably affricated
- A coronal noise source generally dominates most of the release
  - But **not** the final portion of the release
- The transition from dominant alveolar noise source to dominant glottal noise source is smooth
- The proportion of alveolar <> glottal is modulated by phonetic context

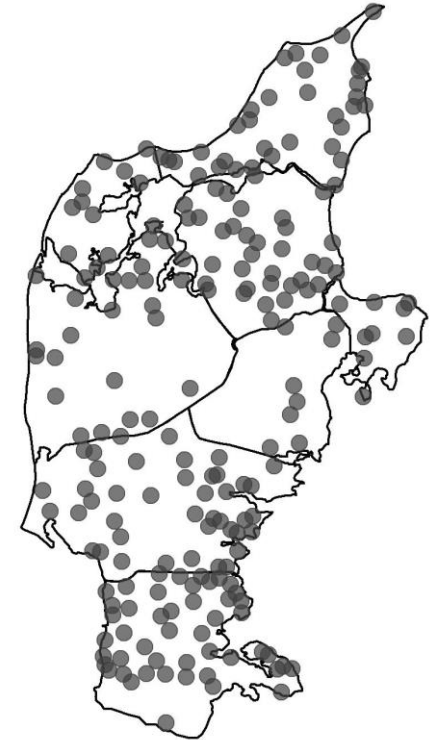
## RQ2: Materials

- Legacy corpus of sociolinguistic interviews with elderly speakers recorded between 1971–1976  
(DS 1971–1976; Goldshtein & Puggaard 2019)
- Recordings from 213 different parishes
- 5,103 /t/ tokens
- 5 ms extracted from each release midpoint
  - Multitaper spectrum generated in R



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- 5,103 /t/ tokens
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  - Multitaper spectrum generated in R
- *Hold up, can't we just model the full /t/ release?*
  - Computationally, sure
  - But how to visualize the results?  
Regional variation in how spectral shape varies over time?



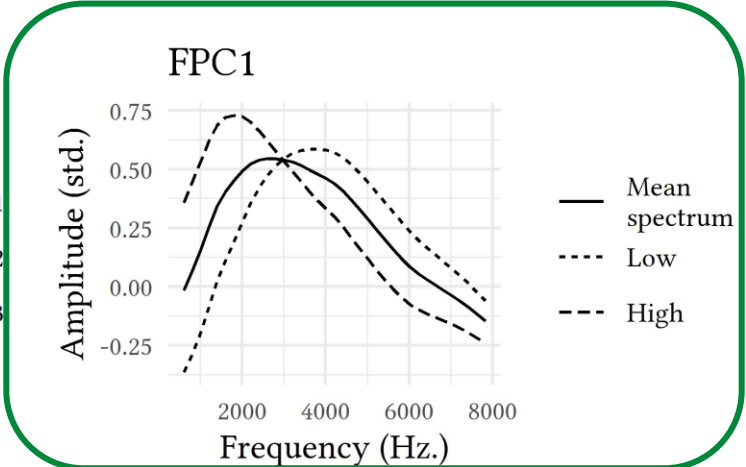
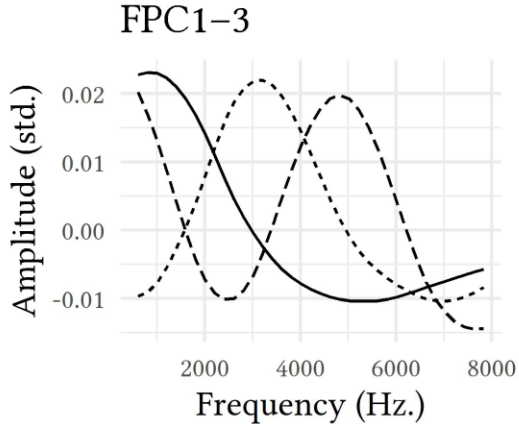
# Functional PCA

- Spectral variance analyzed with functional PCA
  - Identifies main sources of variance
  - Bottom-up approach is particularly suitable here
    - This is exploratory research, and the existing literature doesn't allow for strong predictions
  - Principal components are independent by definition
- FPCA done in R with `fdapace` (Gajardo et al. 2021)
  - PC scores used as dependent variables in spatial GAMMs
    - Predicting PC scores from geography (longitude × latitude), phonetic context, and speaker sex



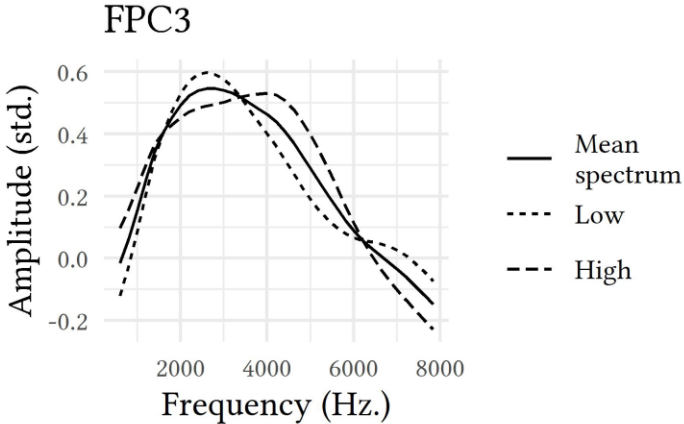
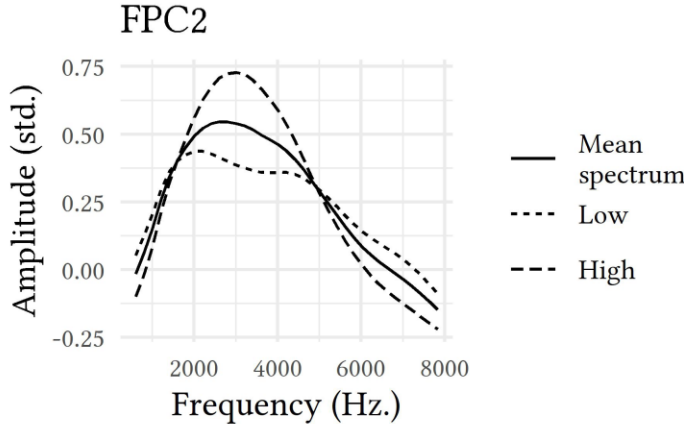
# Results

5 PCs  
account for  
95% of  
variance



58.4%

18.2%



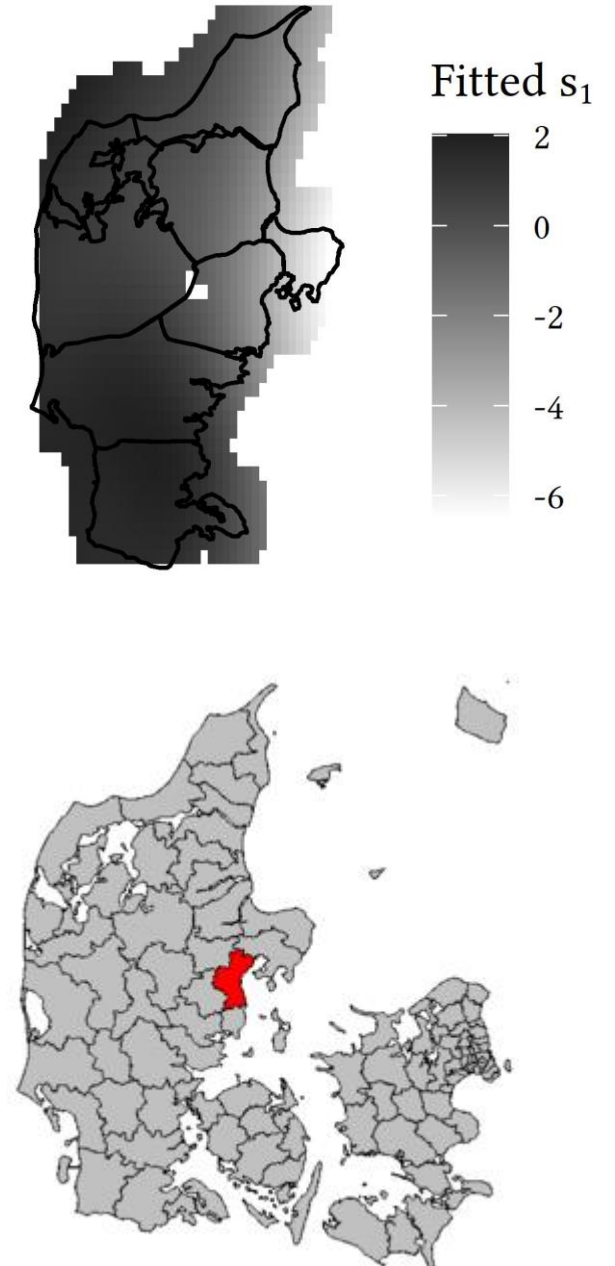
9.3%

# Results

- Negative  $s_1$  (=spectrum reflecting alveolar noise source)
  - Unlikely before low vowels
  - Unlikely before rounded vowels
  - Unlikely before back vowels
  - More likely from female speakers

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  - Unlikely before low vowels
  - Unlikely before rounded vowels
  - Unlikely before back vowels
  - More likely from female speakers
  - More likely in eastern Jutland (particularly Djursland)
    - Could be a traditional feature of this area
    - Could be because this coincides with the biggest city of the peninsula (Aarhus)



# General discussion

- Time-varying spectral characteristics of MSD /t/ releases suggest the presence of both salient affrication and aspiration
  - Smooth transition from one to the other
  - Relative proportion modulated by speaker and phonetic context
- In most traditional Jutland Danish varieties, the /t/ release midpoint does not reflect a coronal noise source
  - Affrication more likely in certain contexts
  - Affrication more likely in eastern Jutland

# General discussion

- FDA allow us to model spectral shape directly
  - Analyzing main sources of variance with FPCA
  - Using spectral shape as a dependent variable with FOSR
- Largely forgoes the problems of other approaches to analyzing the spectrum
  - Bottom-up approach
  - Fairly easy to interpret
  - Familiar scale

# References

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